Atomic Mean-Square Displacements in Proteins by Molecular Dynamics: A Case for Analysis of Variance

Luca Maragliano,* Grazia Cottone,† Lorenzo Cordone,† and Giovanni Ciccotti*

*National Institute for the Physics of Matter and Physics Department, University of Rome, La Sapienza, 00185 Rome, Italy; and [†]National Institute for the Physics of Matter and Department of Physical and Astronomical Sciences,

University of Palermo, 90123 Palermo, Italy

ABSTRACT Information on protein internal motions is usually obtained through the analysis of atomic mean-square displacements, which are a measure of variability of the atomic positions distribution functions. We report a statistical approach to analyze molecular dynamics data on these displacements that is based on probability distribution functions. Using a technique inspired by the analysis of variance, we compute unbiased, reliable mean-square displacements of the atoms and analyze them statistically. We applied this procedure to characterize protein thermostability by comparing the results for a thermophilic enzyme and a mesophilic homolog. In agreement with previous experimental observations, our analysis suggests that the proteins surface regions can play a role in the different thermal behavior.

INTRODUCTION

The characterization of atomic motions in proteins is essential for understanding their biological relevance; indeed, a huge variety of experimental and theoretical work has been devoted to the subject. In their pioneering work, Frauenfelder and his co-workers (Frauenfelder, 1989; Frauenfelder et al., 1979) extracted information on atomic mean-square displacements by exploiting the crystallographic atomic Debye-Waller factor that represents the fractional intensity shift of the diffraction pattern, defined as

$$f_{\rm DW} = exp\left(-2B\frac{\sin^2\theta}{\lambda^2}\right),\tag{1}$$

where λ is the wavelength of incident light, θ the scattering angle, and $B = 8\pi^2 \langle u^2 \rangle$, with $\langle u^2 \rangle$ a measure of atomic disorder, from which the amplitude of the displacements of atomic positions can be obtained. Such information has also been obtained by other methods as Mössbauer spectroscopy (Parak et al., 1982) and neutron scattering (Doster et al., 1989).

From now on, we indicate with $\langle u^2 \rangle$ the mean-square displacements of the atomic positions, i.e., a measure of variability of the distribution functions of the atomic positions. The full form of these distributions is rarely considered, but it is of great relevance to characterize internal atomic motions (Ichiye and Karplus, 1987). The distributions may show only one maximum, i.e., be monomodal, or

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Address reprint requests to Luca Maragliano, National Institute for the Physics of Matter National Research Center on nanoStructures and bioSystems at Surfaces (S3), Physics Dept., University of Modena, via Campi 213/A, 41100 Modena, Italy. Tel.: +39-059-205-5323; Fax: +39-059-367-488; E-mail: maragliano.luca@unimo.it.

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be more complicated, for example with several maxima, that is multimodal. This situation is often encountered in proteins in which, due to conformational changes essential for biological activity, atoms can be delocalized among several sites. When the distribution function of atomic positions is multimodal, the average positions of the atoms are ill defined, as are their mean-square displacements. In this work, we discuss a method to obtain meaningful mean-square displacements of atomic positions in proteins from molecular dynamics (MD) simulations.

We faced this problem while studying the properties of an enzyme extracted from a thermophilic organism. Thermophilic and hyperthermophilic bacteria are organisms that thrive optimally at temperatures higher than 60°C, and in recent years their investigation has attracted wide interest (Gupta, 1993; Jaenicke, 2000a; Kumar and Nussinov, 2001). Proteins extracted from these organisms are stable and working at temperatures at which those obtained from organisms living around room temperature (mesophiles) are known to denature. The general strategy by which these proteins achieve their thermal stability is yet poorly understood. To address this question we applied our approach to two different macromolecules, a thermophilic one and its homolog from a mesophilic organism, and we analyzed data from simulations performed at different temperatures.

Several experimental (Matthews et al., 1987; Jaenicke, 2000a; Kumar and Nussinov, 2001; Querol et al., 1996; Hardy et al., 1994) and simulation (Lazaridis et al., 1997; Tavernelli and Di Iorio, 2001) studies have pointed out that thermophilic proteins should possess a higher degree of rigidity compared to their mesophilic counterparts, which would enable them to better resist to high temperature. However, this seems not to be a general feature of thermophilic proteins. The assumption that the amplitude of atomic mean-square displacements could reflect the rigidity of a molecule (or of groups of atoms) lays on the Lindemann criterion (Lindemann, 1910). Such a criterion states that a crystal melts when the ratio between the atomic

root mean-square displacements and the lattice constant is >0.1. This empirical rule, first established for solids, has been also applied to characterize the dynamics of van der Waals clusters and protein modeling homopolymers (Zhou et al., 1997). Accordingly, we will assume that the larger is the value of the atomic mean-square displacements, the less rigid is the protein. This article is organized as follows: in the next section we introduce our approach to analyze mean-square displacements. In the third section, "Model and Simulation Details", we describe the models of the molecules we simulated, together with details of the simulations. The fourth section contains the results of the application of our method to the two proteins, and in the fifth section we draw our conclusions.

ANALYZING MEAN-SQUARE DISPLACEMENTS

In statistical mechanics, the probability density function for an atom i to be at position \mathbf{r} is defined as

$$P_{i}(\mathbf{r}) \equiv \langle \delta(\mathbf{r}_{i} - \mathbf{r}) \rangle,$$
 (2)

where angular brackets indicate ensemble or, for the ergodic hypothesis, time averages. Some relevant parameters associated with the distribution are the average value of positions,

$$\langle \mathbf{r} \rangle_{i} \equiv \int \mathbf{r} P_{i}(\mathbf{r}) d\mathbf{r} \tag{3}$$

and its variance

$$\langle (\mathbf{r} - \langle \mathbf{r} \rangle_{i})^{2} \rangle_{i} \equiv \int (\mathbf{r} - \langle \mathbf{r} \rangle_{i})^{2} P_{i}(\mathbf{r}) d\mathbf{r} = \langle \mathbf{r}^{2} \rangle_{i} - \langle \mathbf{r} \rangle_{i}^{2}.$$
 (4)

The average value is called a localization measure of the distribution of the population, and tells us where, if ever, we should expect to find the atom, whereas the variance is called a variability measure, and tells us a range for the expected positions. Another important localization measure is the mode, which is defined as the value of \mathbf{r} at which $P_i(\mathbf{r})$ has a maximum. When the distribution $P_i(\mathbf{r})$ has only one maximum, it is said to be monomodal, whereas if it has more than one, it is said to be multimodal. In the latter case, it is not straightforward to estimate the variance, because different methods can bring biased measures. In the following we describe how to obtain reliable (i.e., unbiased) estimates of the variance for the probability distributions functions of atomic positions via molecular dynamics simulations. For each atom, we estimate the probability distribution function with the three-dimensional histogram of coordinates. Before computing histograms, each configuration is corrected for the effects of rigid body translations and rotations of the whole molecule (Kneller, 1991). As an illustration, in Fig. 1, a and b, we show a monomodal and a bimodal distribution, respectively. They pertain to two atoms of the thermophilic protein, the backbone carbon of Trp-316 and the most external nitrogen of the side chain of

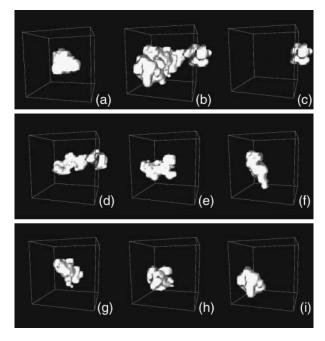


FIGURE 1 Three-dimensional distributions of coordinates for two atoms of $\mathrm{Ss}\beta\mathrm{gly}$ at 360 K. Data were collected over the whole 1.4 ns simulation. (a) Backbone carbon of residue Trp-316. (b) Side-chain nitrogen of residue Gln-103. (c) Same as b, but for the time window 0–200 ps, (d) 200–400 ps, (e) 400–600 ps, (f) 600–800 ps, (g) 800–1000 ps, (h) 1000–1200 ps, and (i) 1200–1400 ps. Boxes of 20 Å side length have been drawn, centered in the average position of the atoms.

Gln-103. Fig. 1, *c*–*i*, shows the distributions of positions for the nitrogen atom of the side chain of Gln-103 calculated over successive time windows of 200 ps along the simulated trajectory. The distributions were obtained for the trajectory at 360 K, which is the working temperature for the thermophilic enzyme (for details of the simulation, see below). As a first estimate of the variance, we compute the mean-square displacements as the following isotropic average, to which we will refer as total mean-square displacements:

$$\langle u_i^2 \rangle_T = \frac{1}{3} \left[\langle x_i^{*2} \rangle_T - \langle x_i^* \rangle_T^2 + \langle y_i^{*2} \rangle_T - \langle y_i^* \rangle_T^2 + \langle z_i^{*2} \rangle_T - \langle z_i^* \rangle_T^2 \right].$$
 (5)

The symbol $\langle \rangle_T$ indicates time averages over the whole trajectory, and $\{r_i^*, i=1,...,N\}$, with N the number of atoms, is the configuration obtained after the correction procedure described above. To define a different estimate, we divide the simulated trajectories in n time blocks of the same length, and calculate displacements as

$$\langle u_{i}^{2} \rangle_{j} = \frac{1}{3} \left[\langle x_{i}^{*2} \rangle_{j} - \langle x_{i}^{*} \rangle_{j}^{2} + \langle y_{i}^{*2} \rangle_{j} - \langle y_{i}^{*} \rangle_{j}^{2} + \langle z_{i}^{*2} \rangle_{j} - \langle z_{i}^{*} \rangle_{j}^{2} \right], \tag{6}$$

where $\langle \rangle_j$, with j=1,...n, indicates a time average over the block j. For a discussion of the proper time-block length chosen, see below in the Results section. Then, we define the mean-square displacements within blocks as the average

$$\langle u_i^2 \rangle_w = \frac{1}{n} \sum_{j=1}^n \langle u_i^2 \rangle_j.$$
 (7)

If an atom has a monomodal distribution, the total and within-blocks displacements will not differ too much, whereas if the distribution is multimodal, they can be significantly different, the total one providing more biased estimate of the variance. In this case, we will consider the within-blocks displacements as the best estimate of the variance. Therefore we calculate and compare the total and within-blocks displacements for each atom, which requires an analysis of variance (Armitage, 1971) for each atom in each simulated trajectory. When the result of the analysis is statistically significant, we conclude that the total meansquare displacement is a biased measure of the variance, and we consider only the within-blocks displacements. To define our method with the highest degree of accuracy, we concentrated only on single atom quantities, avoiding any averaging on structural (i.e., backbone or side chain) or chemical (i.e., residues) groups. The computation of the mean-square displacements for any group of atoms, indeed, requires some consideration of the averaging procedure, which can be the subject of further work.

MODEL AND SIMULATION DETAILS

Using MD simulations, we studied the β -glycosidase protein from Sulfolobus solfataricus (Ss\(\beta\)gly), a hyperthermophilic archaeon that grows at 360 K, and the homolog mesophilic β -glucosidase (C β glu) from *Trifolium repens* (white clover). The crystal structures of the two proteins have been solved by Aguilar et al. (1997) and by Barrett et al. (1995), respectively. The first is a homotetrameric enzyme, in which each monomer, composed of 489 residues, has a molecular mass of 60 kDa; the second is an homodimer, in which each monomer contains 490 residues and has a molecular mass of 62 kDa. The two monomers show a 25% homology. They both belong to the family 1 of the glycosyl hydrolases enzymatic group, whose structure and mechanism have been extensively described (Davies and Henrissat, 1995; Panasik et al., 2000). Their monomers show the same threedimensional fold, referred to as $(\beta \alpha)_8$ barrel structure (Creighton, 1993): eight β -strand patterns are folded in a barrel fashion, and successive β -strands are connected through parts of the polypeptide chain enclosing large α -helix patterns, so to have eight pairs of successive β -strands and α -helices, called $\beta\alpha$ -units. A pictorial view of the three-dimensional structures of the two proteins is shown in Fig. 2. In Fig. 3 is shown the topology diagram of

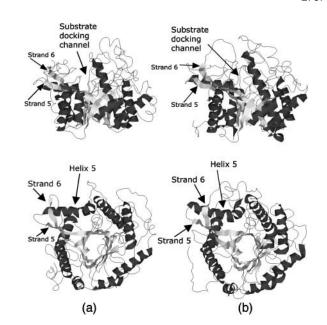


FIGURE 2 Schematic drawings of the $(\beta\alpha)_8$ barrel folded structure of β -glycosidase from *Sulfolobus solfataricus* (Ss β gly) (a) and β -glucosidase from *Trifolium repens* (white clover) (C β glu). (b) Upper row, side view; lower row, top view. Strands and helices of the barrel are shown as light shaded and dark shaded areas, respectively.

both proteins. The connections between subsequent $\beta\alpha$ -repeats are located at the bottom of the barrel and are all composed of few residues, with the exception, in both molecules, of the one connecting α -helix 5 and β -strand 6. In both proteins, connections between the β -strand and the α -helix of each unit (at the top of the barrel) are more elaborate, containing extra secondary structure elements, not explicitly shown in Figs. 2 and 3, which shield the barrel structures from the solvent (Aguilar et al., 1997; Barrett et al., 1995). The thermophilic behavior of Ss β gly has been clearly characterized (Moracci et al., 2001): it shows optimal activity above 358 K, temperature at which its half-life is 48 h.

MD simulations were performed using DLPROTEIN (Melchionna and Cozzini, 2001). The force field used is CHARMM22 (MacKerell et al., 1998), with the SPC/E model for water molecules (Berendsen et al., 1983). The initial coordinates of thermophilic Ss β gly and mesophilic C β glu were obtained from the crystal structures registered in the Protein Data Bank of the Research Collaboratory for Structural Bioinformatics with codes 1gow (Aguilar et al., 1997) and 1cbg (Barrett et al., 1995).

All hydrogen atoms were explicitly added, obtaining a total of 7819 atoms for Ss β gly and 7838 atoms for C β glu. Each of the two molecules was then put in a rectangular box filled with water solvent, using an equilibrated SPC/E modeled water configuration as the building block and removing water molecules whose atoms were <1.8 Å from any protein atom. The final number of water molecules in the systems was 7258 for Ss β gly and 7116 for C β glu simulations. To obtain neutrality, in the Ss β gly system we

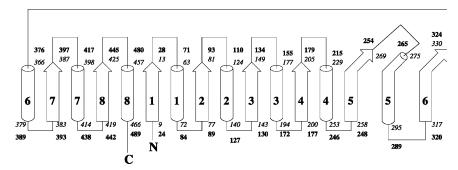


FIGURE 3 Topology diagram of the folded $(\beta\alpha)_8$ barrel structure of $Ss\beta gly$ and $C\beta glu$. Helices are shown as cylinders, and strands are shown as arrows. Small secondary structure elements present in intra- and inter- $\beta\alpha$ -units connections are not shown. The number of the first and last residue in each secondary structure element is indicated, starting from the amino head of the chain and ending with the carboxy tail. Italic numbers refer to $Ss\beta gly$ residues and bold numbers to $C\beta glu$.

replaced five randomly chosen water molecules with four calcium ions and one chlorine ion, whereas in the C β glu system, three water molecules were replaced by three chlorine ions. The two systems were energy minimized, quenching them at zero temperature. For $Ss\beta gly$, equilibration runs were performed with Berendsen quasi-constant pressure (P = 1 kbar) and temperature technique (Berendsen and Van Gusteren, 1984), with temperatures of 300 K and 360 K, and coupling constants of 0.4 ps and 4 ps for the "thermostat" and the "barostat", respectively. The length of these runs was 50 ps at 300 K and 80 ps at 360 K. Then we continued to equilibrate in the canonical ensemble for 250 ps at 360 K and 200 ps at 300 K, by coupling the system with a Nosè thermostat (Nosè, 1984) with a time constant of 0.4 ps. The simulations for data collection were also performed in the canonical ensemble, and consisted of trajectories of 1.4 ns at 360 K and 300 K. For C\(\beta\)glu, equilibration runs were performed with the Berendsen quasi-constant pressure (P = 1 kbar) constant temperature technique (Berendsen and Van Gusteren, 1984) with temperatures of 300 K and 360 K, and coupling constants of 0.5 ps and 5 ps for the "thermostat" and the "barostat", respectively. These runs were 60 ps long at 300 K and 360 K. Then we continued equilibration with runs of 250 ps in the canonical ensemble with the Nosè thermostat (Nosè, 1984) and a time constant of 0.4 ps. Data were collected, during simulations in the canonical ensemble, from trajectories of 1.2 ns at 300 K and 1.4 ns at 360 K.

In all simulations, periodic boundary conditions were used (Frenkel and Smit, 2002). Van der Waals interactions were cut off at a distance of 10 Å, whereas electrostatic interactions were calculated by Ewald sums using the smooth particle mesh Ewald method (Esmann et al., 1995). The cutoff of the real space part was 10 Å, and the Ewald α -parameter was set to 0.31 for Ss β gly and to 0.36 for C β glu. Eighth order cubic splines were used for interpolation, with grids of 75 \times 75 \times 65 for Ss β gly and 75 \times 85 \times 75 for C β glu. All chemical bonds in the molecules were kept fixed using the SHAKE algorithm (Ryckaert et al., 1977, Ciccotti and Ryckaert, 1986). Equations of motion were integrated with the velocity Verlet scheme (Andersen, 1983, Tuckerman et al., 1992) with a time step of 1 fs. Coordinates were saved every 100 fs for data analysis.

RESULTS

As a first step of our analysis, we need to determine the suitable time-block length to compute the mean-square displacements within blocks defined in Eq. 7. To this purpose we calculated, for the 360-K trajectory of C β glu, the distribution of atomic mean-square displacements within blocks for several block lengths L, say 50, 100, 150, 175, 200, 250, 300, 350, 400, 600 and 1400 ps. We indicate with $\{f_j^L\}_{j=1,\dots,\mathcal{N}}$ the frequency distribution of the mean-square displacements within blocks corresponding to a given block length L, \mathcal{N} being the number of class intervals we considered, and with n_L the total number of block lengths (and hence of different distributions). Then, we calculate a reference distribution, which we indicate as $\{\bar{f}\}\$, defined as follows: given the set of all the values f_i^L , with $j = 1, ..., \mathcal{N}$ and $L = 1, ..., n_L$, we calculate the distributions $\{f_i^{\text{max}}\}$ and $\{f_i^{\min}\}$, defined such as, \forall_i ,

$$f_{\mathbf{j}}^{\max} = \max_{L \in \{1, \dots, n_{\mathbf{l}}\}} f_{\mathbf{j}}^{\mathbf{L}} \tag{8}$$

and

$$f_{j}^{\min} = \min_{L \in \{1, \dots, n_L\}} f_{j}^{L},$$
 (9)

respectively; then, we take

$$\bar{f_{\rm j}} = \frac{f_{\rm j}^{\rm max} + f_{\rm j}^{\rm min}}{2}.$$
 (10)

Hence, by definition, $\{\bar{f}\}$ is the distribution of the middle values in the range of all the f_j^L values we have. This definition of the reference distribution should ensure that our results do not depend on the total simulation length, since $\{f_j^{\max}\}$ and $\{f_j^{\min}\}$ should not vary sizably with it. We will return to this point below. Now, for each distribution, we calculated the value

$$X^{2} = \sum_{j=1}^{\mathcal{N}} \left(\frac{f_{j}^{L} - \bar{f}_{j}}{\sigma_{j}} \right)^{2}, \tag{11}$$

where

$$\sigma_{j}^{2} = \frac{1}{n_{L} - 1} \sum_{L=1}^{n_{L}} (f_{j}^{L} - \bar{f_{j}})^{2}.$$
 (12)

If we could assume that the different values f_i , corresponding to different values of L, were statistically independent, X^2 would be a variable χ^2 with \mathcal{N} -1 degrees of freedom. This hypothesis is, however, not fully plausible. In Fig. 4 (circles), we plot the X^2 values obtained for the different block lengths. The stability region between the values 175 and 350 ps tells us that the differences between the distributions for these block lengths are small, and so we take 200 ps as a proper block length for the calculation of atomic mean-square displacements within blocks. To ensure that this result does not depend on the total simulation length, we should repeat the test for different total lengths. Increasing considerably the simulation length would be too time demanding, and so we did the test for a simulation length of 700 ps. In Fig. 4 (diamonds), we plot the X^2 values obtained for the different block lengths in the case of 700 ps total block length. The distributions $\{f_i^{\text{max}}\}$ and $\{f_i^{\text{min}}\}$ are now calculated using the set of distributions with L = 50, 100, 150, 175, 200, 250, 300, 350, 400, and 700 ps, whereas the reference distribution is calculated again using Eq. 10. As it can be observed, there is a stability region between the values 100 and 250 ps. Since 200 ps is in the center of this range, it turns out again that it is a suitable block length for the calculation of atomic mean-square displacements within blocks. We did this test for the C β glu trajectory at 360 K, for which a larger variability of the mean-square displacements with the time-block length is expected. Accordingly, the obtained value must be suitable also for the other trajectories.

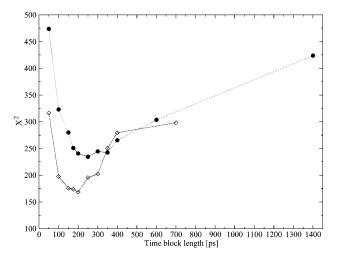


FIGURE 4 Values of X^2 variable (Eq. 9) for the distributions of withinblocks mean-square displacements with different time-block lengths calculated for C β glu at 360 K considering the whole 1.4-ns long trajectory (\bullet) and the first 700 ps (\diamondsuit).

To perform the analysis of variance, we calculated the total and within-blocks mean-square displacements for all the atoms of $Ss\beta gly$ and $C\beta glu$ at 360 K and at 300 K. Figs. 5 and 6, respectively, show the distributions of the total and within-blocks displacements for each protein at both temperatures. In Table 1 are reported the average values, modes, and variances of these distributions. The distributions of total and within-blocks displacements are different, as evident by direct observation and by comparing their parameters. To prove further these differences, we compared them basing on an F variable test on their average values. For each protein at each temperature, we took

$$F = \frac{\overline{\langle u_i^2 \rangle}_T}{\overline{\langle u_i^2 \rangle}_W}, \tag{13}$$

where bars indicate the average values of the distributions of displacements. The result is always significant at the level of 5%. That is, the two measures are not homogeneous. Since the total mean-square displacements are a biased estimate of the variance, we take the within-blocks mean-square displacements as an estimate for the variance of the distribution of atomic positions. Another advantage of using the withinblocks mean-square displacements is that they are robust in time, that is, their values do not depend strongly on the total simulation time length over which they are calculated. To show this property, we calculated the total and within-blocks mean-square displacements for the side-chain N of residue Gln-103 of thermophilic Ss β gly for different simulation lengths. Data were taken from the simulation at 360 K. In Fig. 7, we plot our results for the total and within-blocks displacement. As evident, the total mean-square displacements are always considerably larger than the within-blocks ones. Since they are both estimates of the same quantity, this

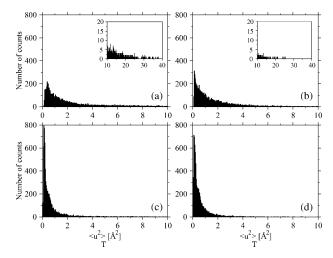


FIGURE 5 Distributions of total mean-square displacements (Eq. 5) for the two proteins: (a) $C\beta$ glu at 360 K, (b) $Ss\beta$ gly at 360 K, (c) $C\beta$ glu at 300 K, and (d) $Ss\beta$ gly at 300 K. Insets show the tails of the distributions; note the different scales. Class intervals are chosen 0.038 Å² tick.

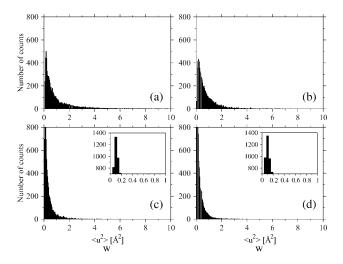


FIGURE 6 Distributions of the mean-square displacements within blocks (Eq.7) for the two proteins: (a) $C\beta$ glu at 360 K, (b) $Ss\beta$ gly at 360 K, (c) $C\beta$ glu at 300 K, and (d) $Ss\beta$ gly at 300 K. Insets show the peaks of the distributions; note the different scales. Class intervals are chosen 0.038 Å² tick.

confirms that the total mean-square displacements are a biased estimate of the variance of the distribution of atomic positions. Furthermore, the total displacements strongly fluctuate when varying the simulation length, whereas the within-blocks displacements become quickly stationary. It is interesting to correlate these results with the distribution of positions for the same atom, plotted in Fig. 1, c-i. The boost obtained for the total displacements value in Fig. 7, when going from 200 to 400 ps and 600ps, is clearly due to the extension of the region visited by the atom in the 200–400 ps time slice (Fig. 1 d). By computing the total mean-square displacement for increasing time lengths, the results are biased by this initial value. At variance, from the definition of the within-blocks displacement (Eq. 7), it is clear that the averaging over the different 200-ps-long blocks provides a measure of the local variability of the distribution of atomic positions.

It is important to mention here that our analysis method is not aimed at canceling out the long time dynamics of protein atoms; rather, it stresses that the mean-square displacements are quantities that cannot be computed straightforwardly. Indeed, for a multimodal distribution of positions, the total mean-square displacements would necessarily result in biased variability measures, associated with ill-defined localization sites, whereas variability measures must only be associated to effective localization sites. A multimodal distribution of positions occurs when, during a certain time, an atom is delocalized between several metastable sites. If this is the case, only local variability measures can be calculated, that is, displacements within the localization sites. From our analysis, it turns out that 200 ps is a proper time-block length to measure this variability. If we do not reduce to local variability measures, due to the change in localization site, we obtain oversized variability measures.

Once established how to calculate mean-square displacements, it has physical meaning to study how they behave when varying the temperature. The molecules we simulated form, in their native configuration, tetramers and dimers. By simulating only the monomers, we could obtain a different pattern of the mean-square displacements for the atoms in the residues located at the intersubunit surface. However, a comparison of results for the two different molecules on the same monomer basis helps in capturing essential features and understanding their different behavior with temperature (Bismuto et al., 2002).

In the literature, results about comparison of rigidity between thermophilic and mesophilic homologs are controversial. Lazaridis et al. (1997) have shown by MD analysis that, at 300 K, a very small hyperthermophilic rubredoxin exhibits higher rigidity than a mesophilic homolog at the same temperature. This suggestion has subsequently been questioned, see e.g., Jaenicke (2000b); moreover, Fitter and Heberle (2000), basing their findings on neutron scattering measurements, reported that on a short timescale (0.1 ns) thermophilic α -amylase, a $\beta\alpha$ -barrel glycosyl hydrolase as Ss β gly and C β glu, is less rigid than its mesophilic counterpart. Colombo and Merz (1999) using molecular dynamics simulations, studied the structural equilibrium displacements (i.e., motions in the hundreds of picoseconds timescale) of a mesophilic subtilisin and a thermophilic homolog. The authors reported that although at room temperature the two molecules show similar flexibility, at higher temperature (350 K) the thermophilic protein has an enhanced flexibility.

The analysis of the distributions of mean-square displacements within blocks for the two proteins points out that at 300 K (Fig. 6, c and d, and parameters in Table 1), the modes are equal, although average values and the variances differ

TABLE 1 Parameters of the distributions of atomic mean-square displacements

		Total mean-square displacements $\langle u_{\rm i}^2 \rangle_{\rm T}$			Mean-square displacements within blocks $\langle u_{\rm i}^2 \rangle_{\rm w}$		
		Average value	Mode	Variance [Å ⁴]	Average value	Mode	Variance [Å ⁴]
Ssβgly	360 K	1.82	0.15	5.23	0.76	0.19	0.60
	300 K	0.61	0.11	0.73	0.32	0.11	0.13
Cβglu	360 K	3.24	0.42	20.16	1.05	0.19	1.67
	300 K	0.86	0.15	2.99	0.37	0.11	0.22

All data are in $Å^2$, except where explicitly written.

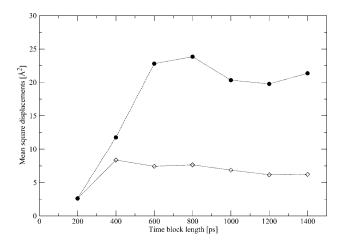


FIGURE 7 Total (\bullet) and within-blocks (\diamond) mean-square displacements for side-chain nitrogen of residue Gln-103 of SS β gly at different total simulation length. Data were taken from the 360-K simulation.

by 15% and 65%, the thermophilic protein showing smaller values. At 360 K (Fig. 6, a and b, and Table 1), the modes are still the same, although the average values differ by $\sim 40\%$, the thermophilic protein showing again smaller values, and the variance of the distribution for the mesophilic is 2.8 times that of thermophilic. More insight can be obtained by plotting the difference between the two distributions at each temperature (Fig. 8). At both temperatures, this quantity oscillates rapidly around zero, implying that it is difficult to extract unambiguous information from the distributions. However, we can observe a signal, small with respect to the amplitudes of the oscillations, but sizable. This signal shows that the distribution for the thermophilic protein is more populated at low fluctuation values, whereas that of the mesophilic is more populated at values $> 1.5 \text{ Å}^2$. This effect, hardly seen at 300 K, is better evident at 360 K (Fig. 8 b).

It is relevant to determine the atoms that contribute to this difference, and if they are located in peculiar regions of the molecules. In C β glu, the 79% of atoms showing displacements of this entity are side-chain atoms, whereas in $Ss\beta gly$ this fraction is 92%. This means that at 360 K in C β glu, there are more backbone atoms with large values of mean-square displacements. We found that they belong to residues located in segments of the polypeptide chain with very poor secondary structure organization, and are more exposed to the solvent than the remaining part of the chain. Regions of this kind are, for example, in C β glu from the N-terminus to residue 64, or the loop region of residues 200-216, whereas for Ss β gly, from residue 464 to the C-terminus, or the loop region formed by residues 212-225. They are the intra- and inter- $\beta\alpha$ -units connections (see Fig. 3). These parts might be involved in the onset of the denaturation process, characterized by the falling apart of the external α -helices. The larger displacements could hence reflect the onset of these largescale motions.

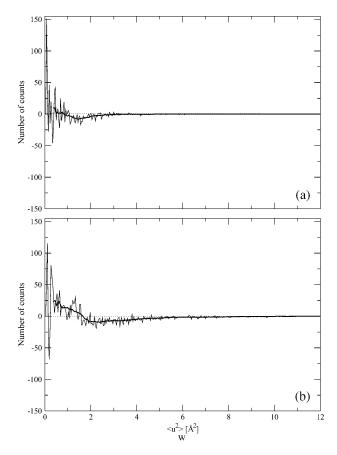


FIGURE 8 Differences between the $Ss\beta gly$ (thermophile) and $C\beta glu$ (mesophile) distributions of the mean-square displacements within blocks at 300 K (a) and 360 K (b). The thick lines connect points, each one calculated as the average of 20 successive data points.

CONCLUSIONS

We have reported a statistical approach to analyze molecular dynamics data on the displacements of atomic positions in proteins. Our method is based on atomic probability density functions of positions. These functions can be estimated by computing three-dimensional histograms of atomic coordinates obtained from simulated trajectories. With a technique inspired by the analysis of variance, we introduce an unbiased procedure to compute mean-square displacements of atoms. These displacements are in turn a random variable over the sample of all atoms, and we analyze them statistically. We applied this analysis to try a characterization of thermostability, and, to this end, compared a thermophilic protein, the β -glycosidase from S. solfataricus (Ss β gly), with its mesophilic homolog, the β -glucosidase (C β glu) from T. repens (white clover). By comparing the distributions of these displacements in Ss β gly with those of C β glu at the same temperatures, we conclude that there are some differences between the two proteins, and some dissimilarity may be noted in the connection regions of the $(\alpha\beta)$ barrel structures, which might be a signature of the different behavior of the two molecules at high temperature. Indeed,

these structures, which are more exposed to the solvent than the rest of the chain, could have a role in the onset of the denaturation process, characterized by the falling apart of external α -helices, which shield the barrel from the solvent (Bismuto et al., 2003).

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